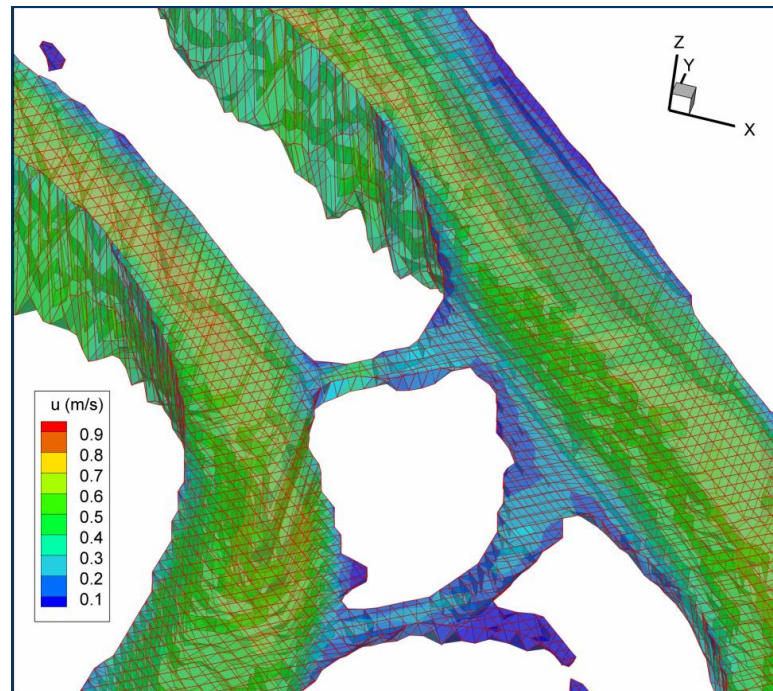


# Modelling of flow and sediment transport in rivers and freshwater deltas



Foto: Fjellanger Widerøe AS ©



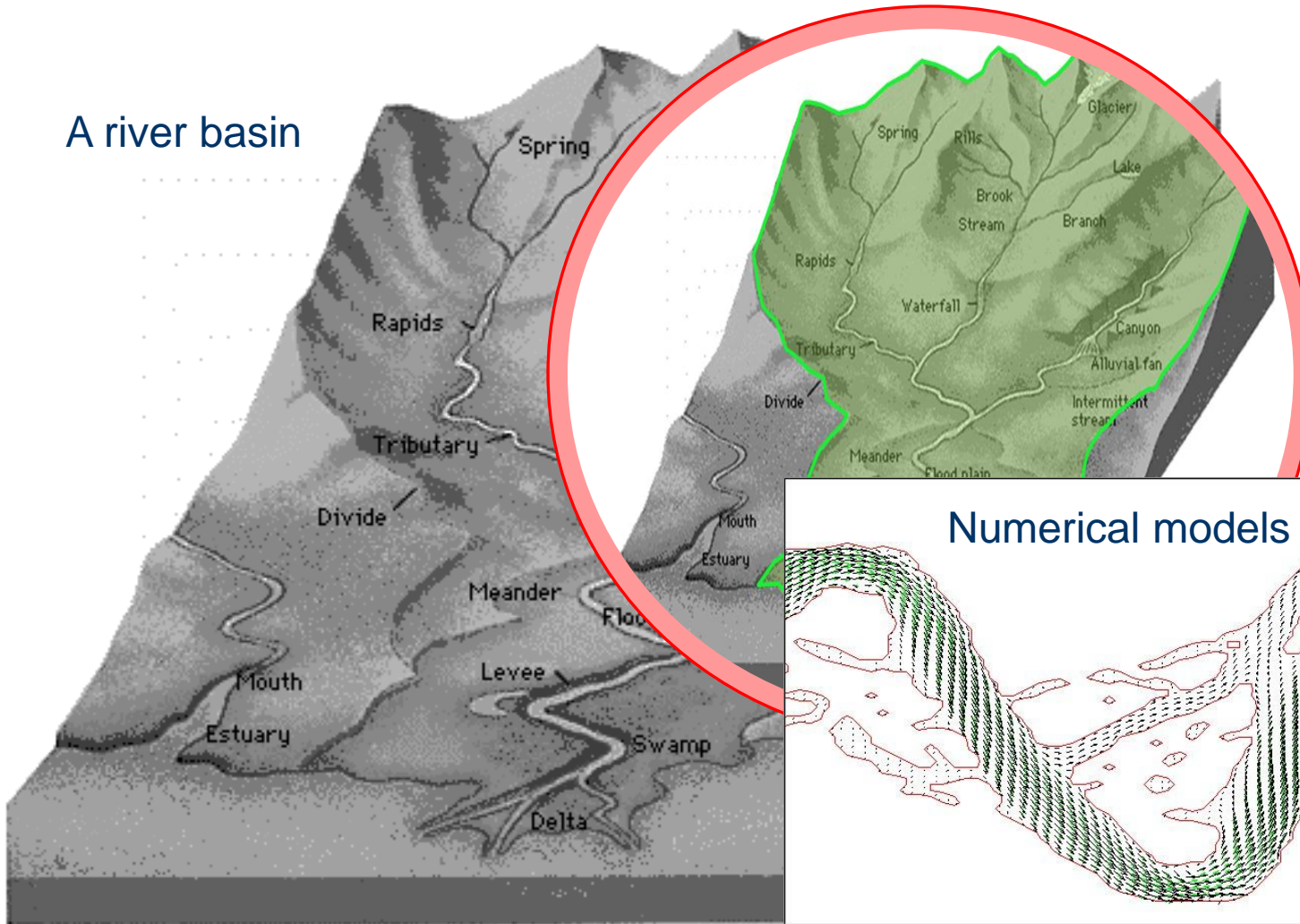
**Peggy Zinke**

with contributions from Norwegian and international project partners

# Outline

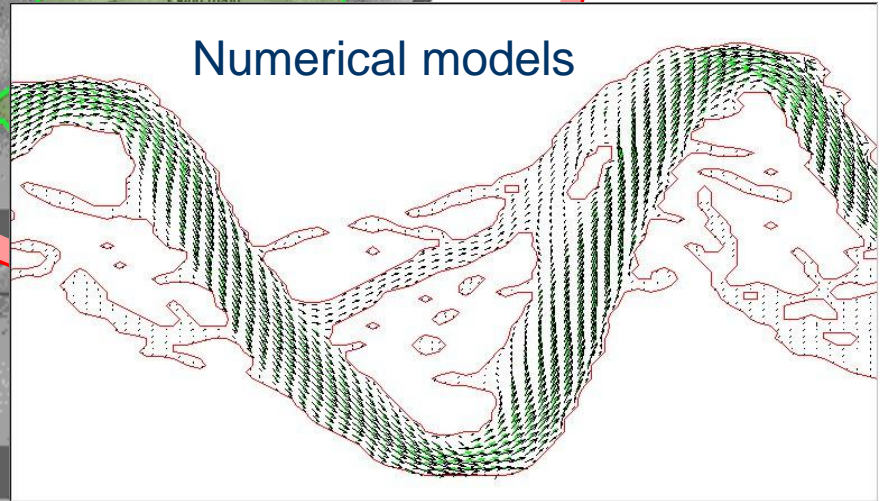
1. Introduction
2. Basic ideas of flow and sediment modelling in rivers
3. Some examples for flow and sediment models
4. RANS Modelling study for Lake Øyeren's delta
5. Short summary

A river basin

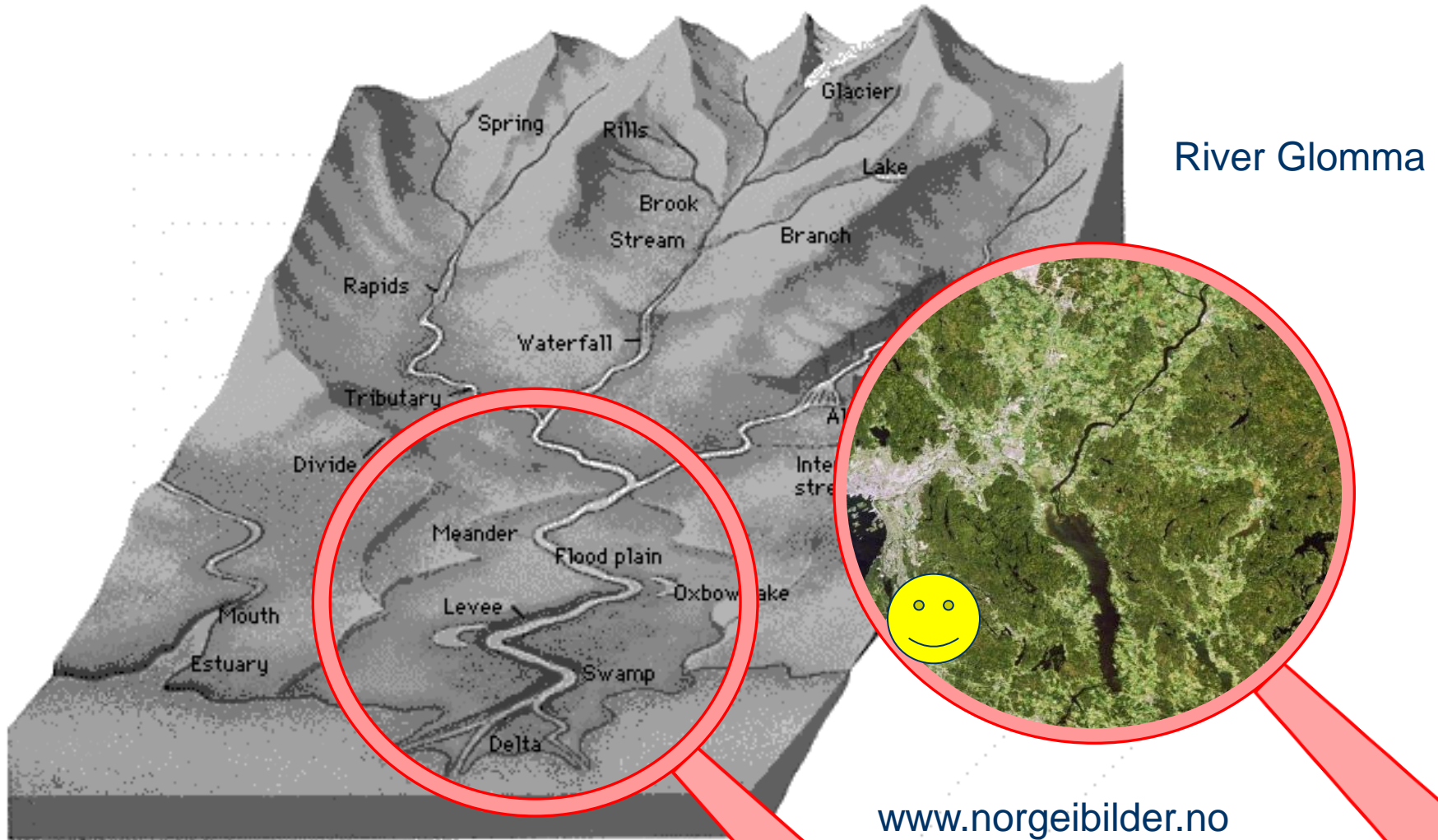


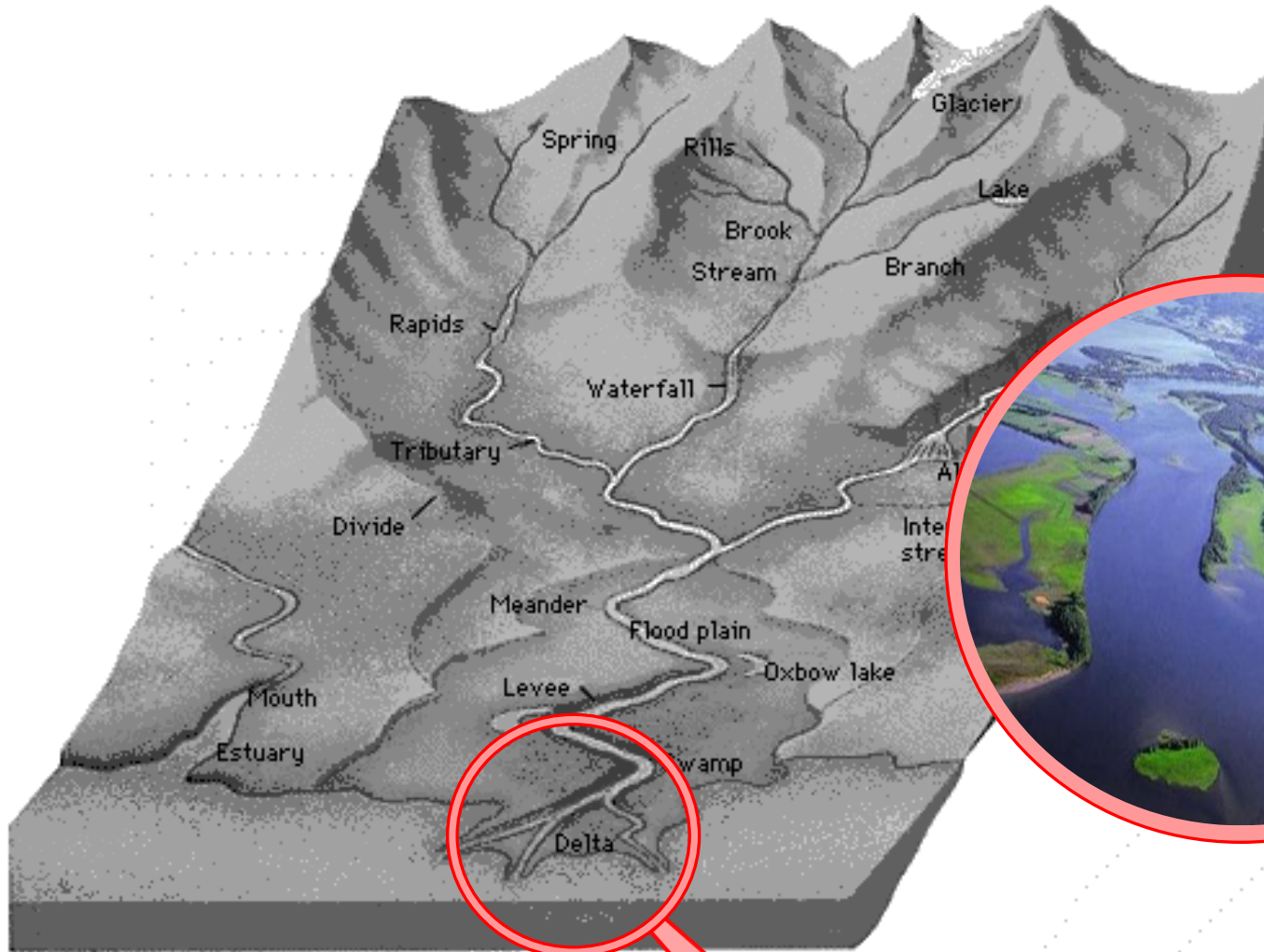
Physical models

Numerical models



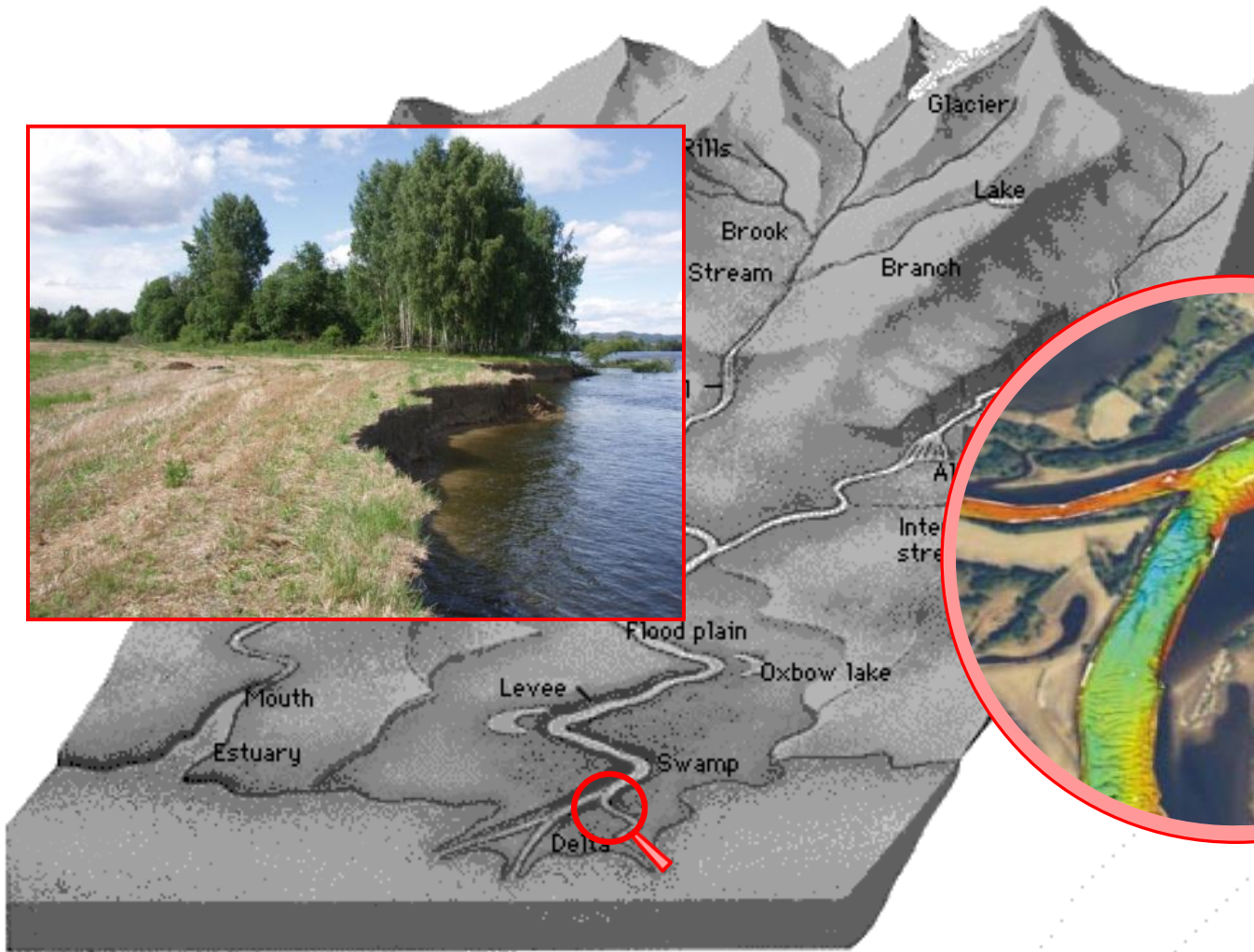






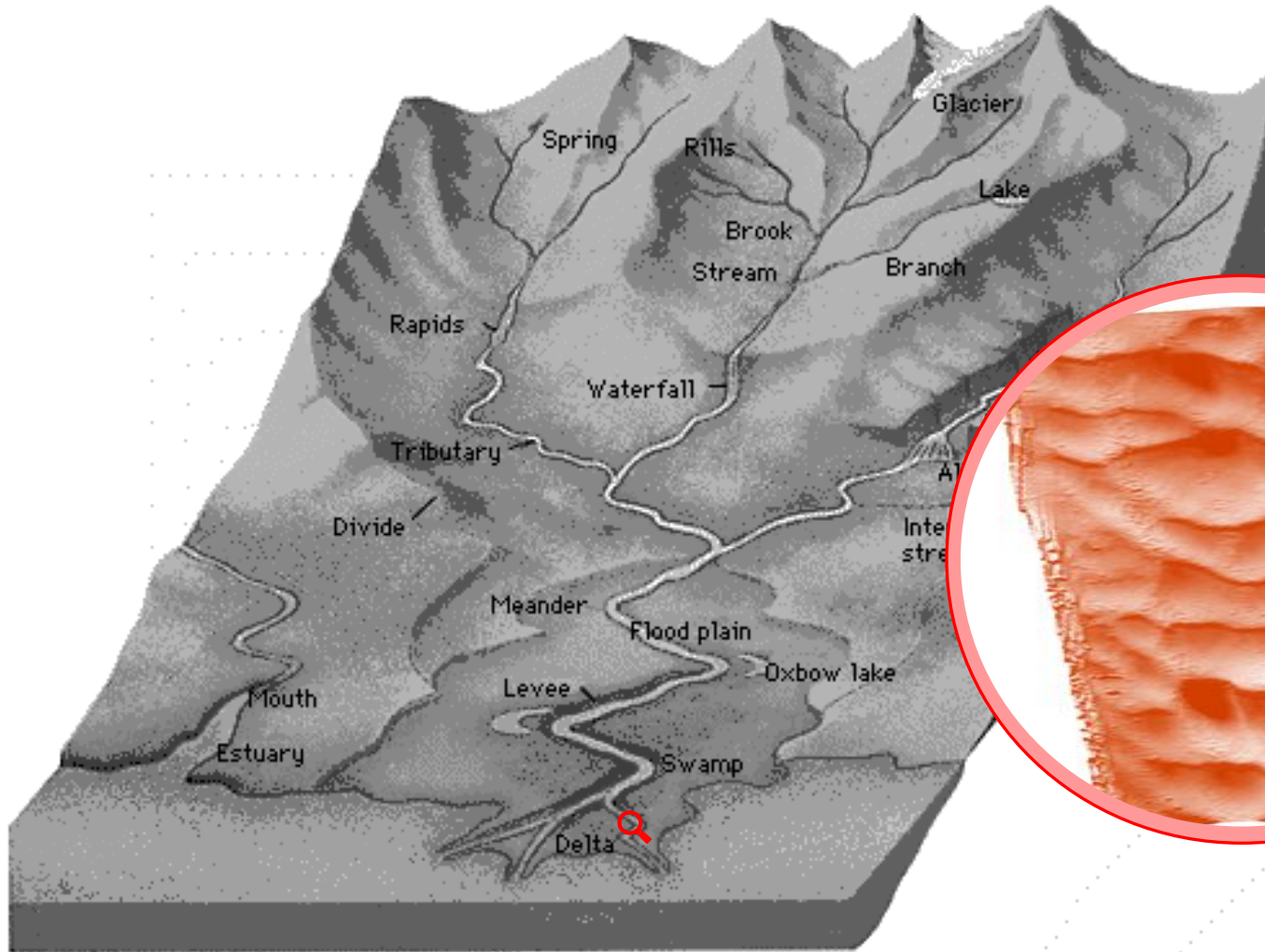
Lake Øyeren's delta



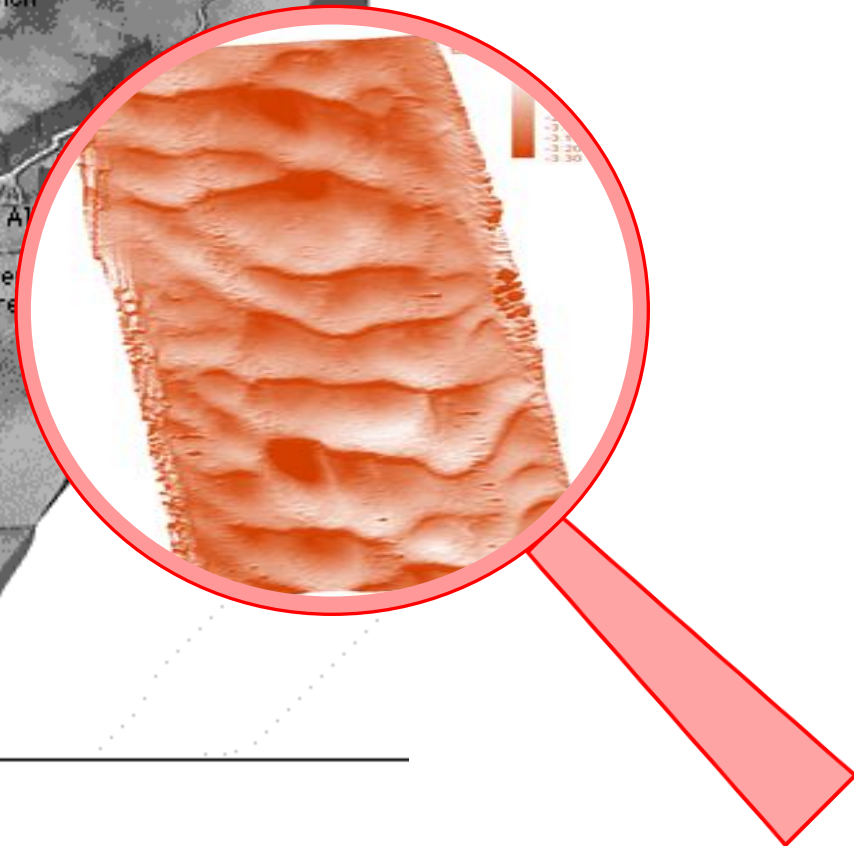


Single channels, bifurcations and confluences





Bedforms of a sand-bed channel





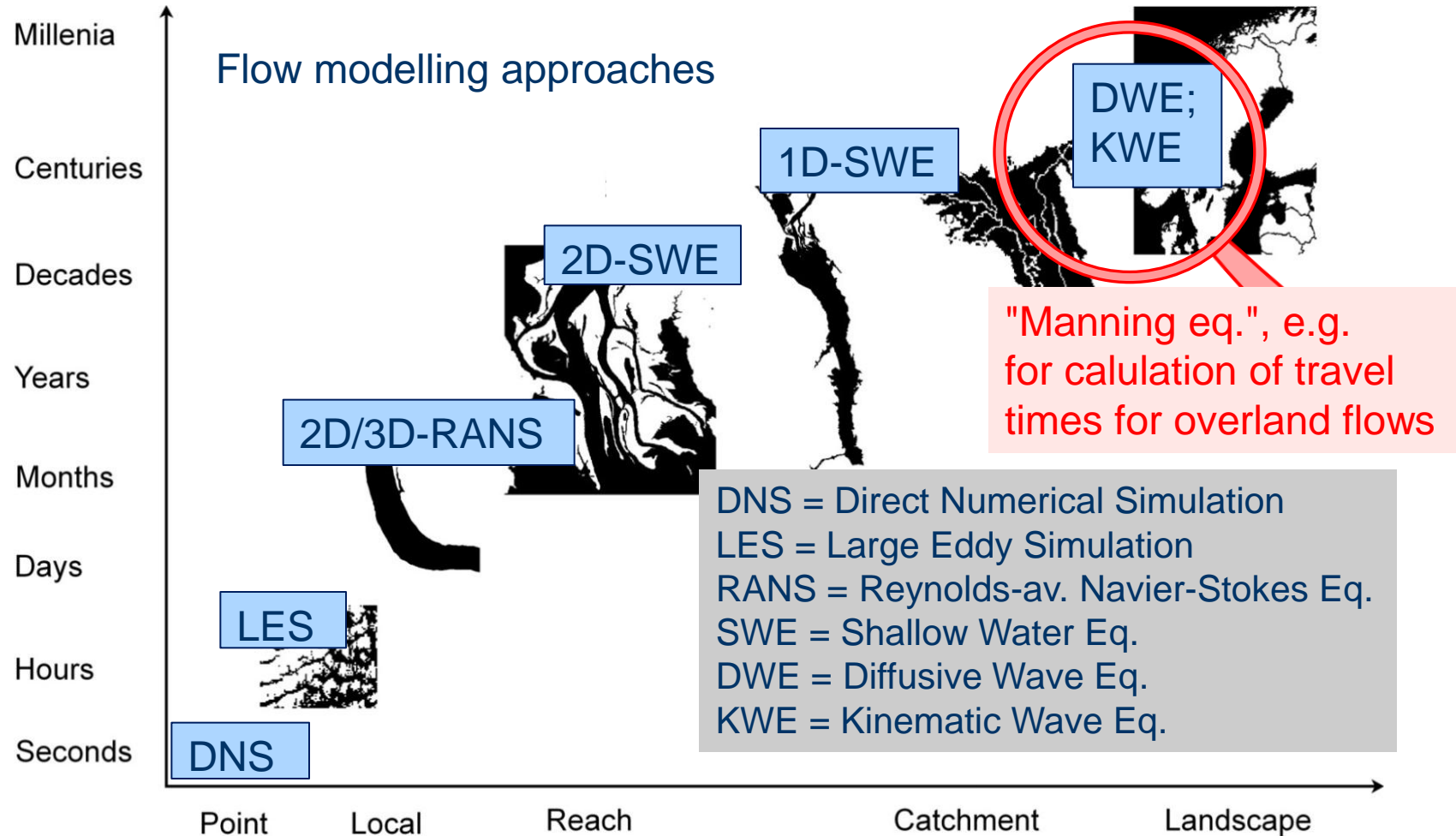
Computational effort & resolution requirements

Degree of averaging & simplification

## Modelling of flow and sediment transport in rivers

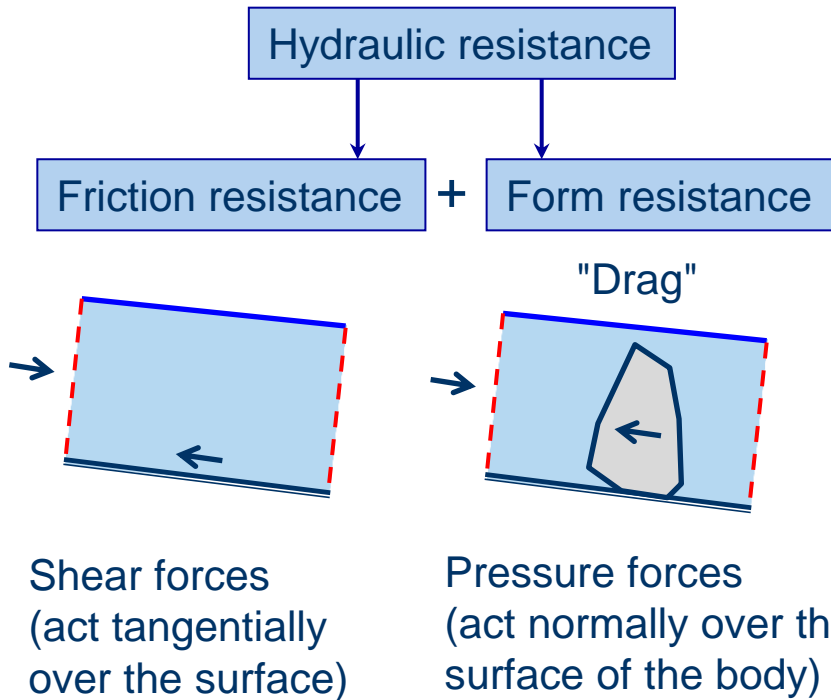


## 2. Basic ideas of flow and sediment modelling

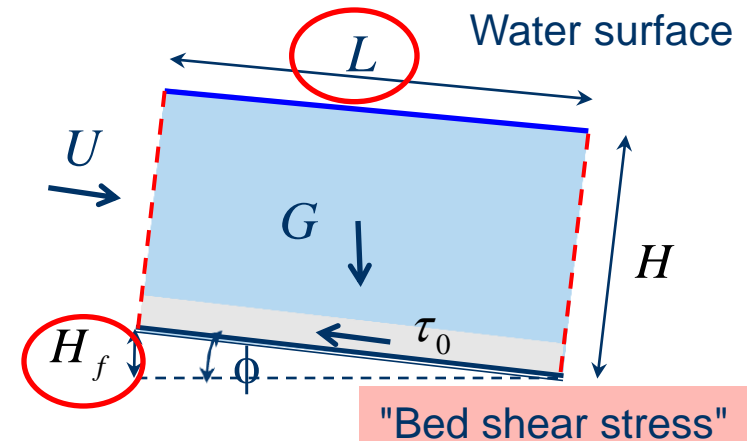


Hydraulic resistance =  
the pressure (head) loss per flow rate  
because of energy dissipation

Classical division into two compounds:



The most simple model:



Gravity force component = Shear force on the river bed

$\tau_0 \propto U^2$  For rough turbulent flow

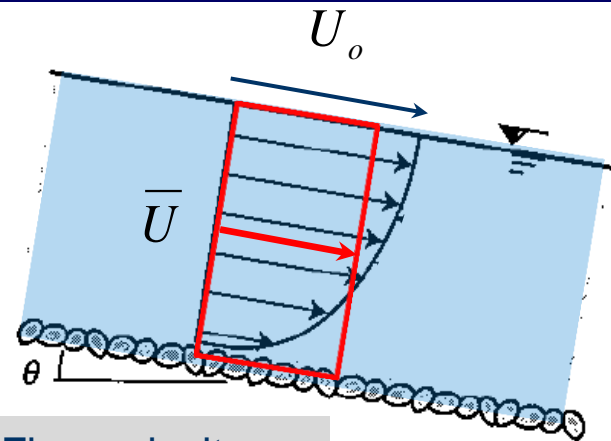
Skin friction coefficient  $C_f$  = the bed shear stress normalized by a reference velocity, e.g. bulk velocity  $\bar{U}$

$$C_f = \frac{\tau_0}{\frac{1}{2} \rho \bar{U}^2}$$

$$\tau_0 = R \cdot \rho \cdot g \cdot S$$

"Bed shear stress"

$$\bar{U} = \sqrt{\frac{R \cdot \rho \cdot g \cdot S}{C_f \cdot \frac{1}{2} \rho}} = \sqrt{\frac{2g}{C_f}} \sqrt{R \cdot S} = C \sqrt{R \cdot S}$$



U = Flow velocity  
R = Hydraulic radius  
S = Slope

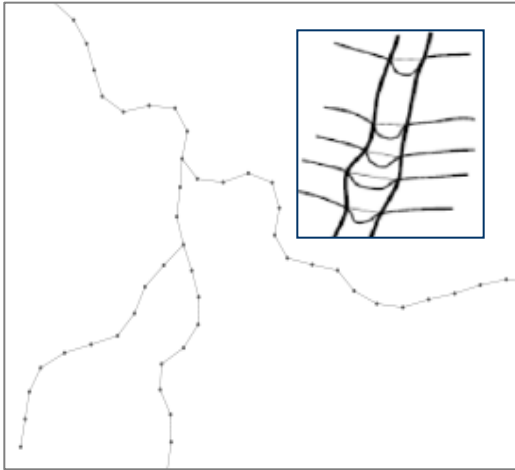
Chezy	Manning	Strickler	Darcy-Weisbach
$U = C \sqrt{RS}$	$U = \frac{1}{n} R^{\frac{2}{3}} S^{\frac{1}{2}}$	$U = k_{ST} R^{\frac{2}{3}} S^{\frac{1}{2}}$	$U = \sqrt{\frac{1}{\lambda} 8gRS}$
C = Chezy coefficient	n = Manning coefficient	$k_{ST}$ = Strickler coefficient	$\lambda$ = Darcy-Weisbach friction factor

**For steady uniform flow!!!**

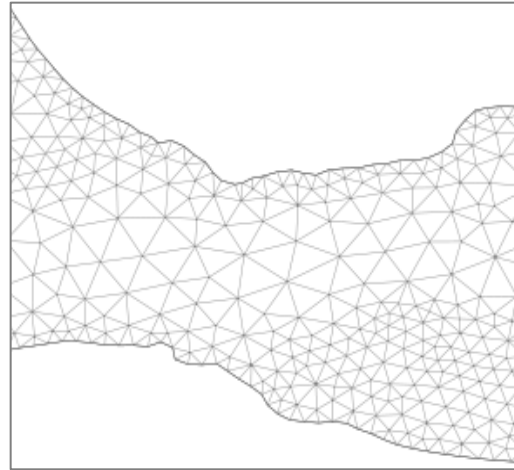
*Overall resistance values; Friction factors*



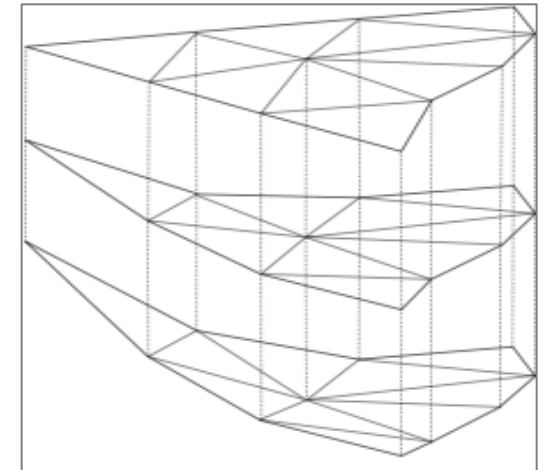
## 1D, 2D and 3D hydrodynamic models



a) 1D mesh



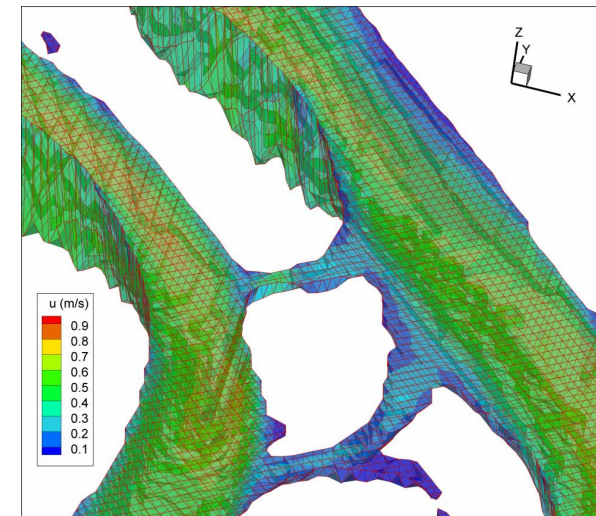
b) 2D mesh



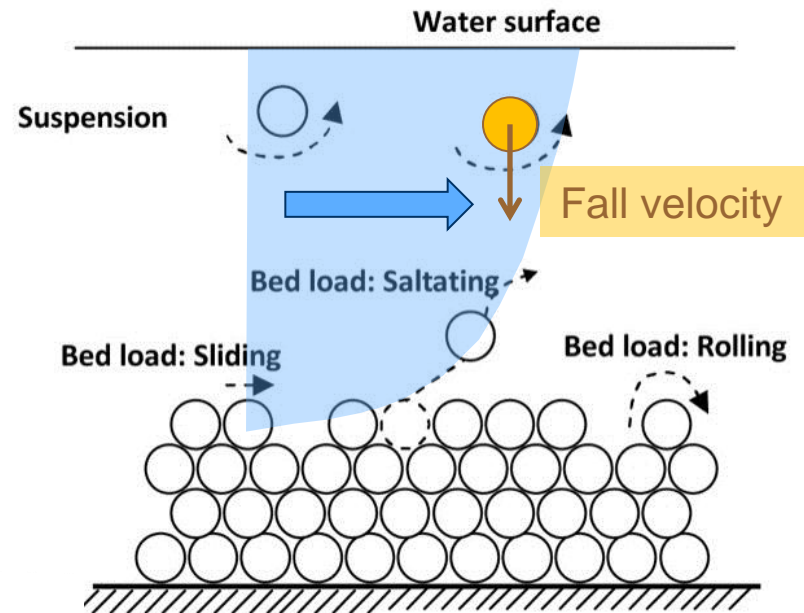
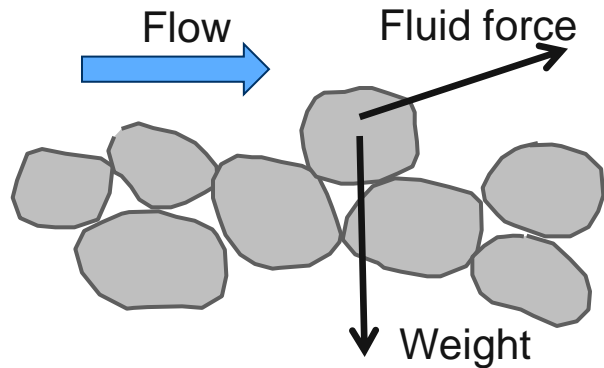
c) 3D mesh

Computation of average flow parameters

- a) Over the cross-section (1D)
- b) Over the vertical, per model cell (2D)
- c) Per model cell (3D)

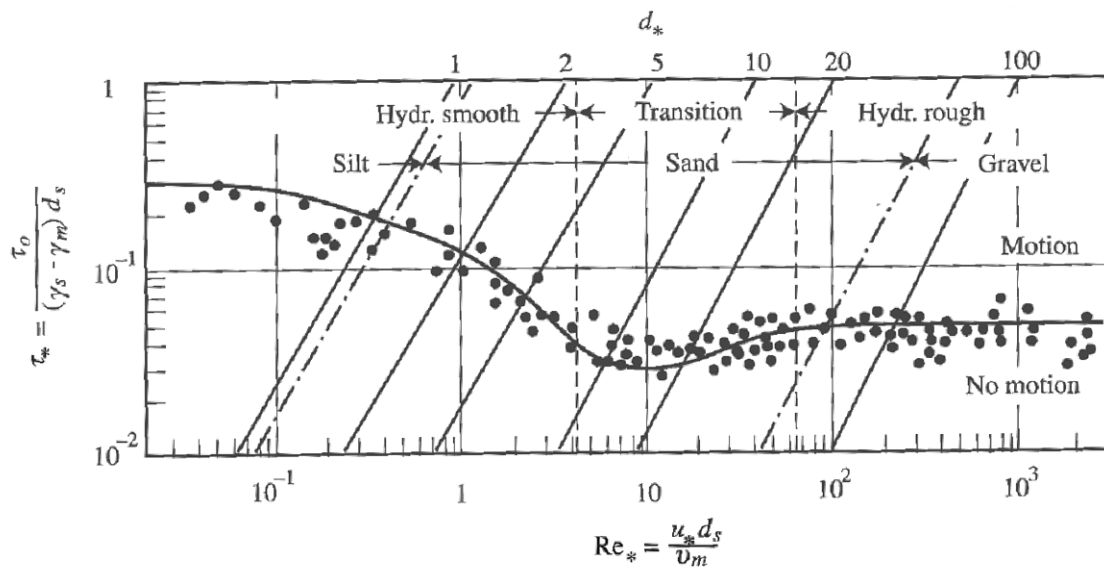


## Sediment modelling



Particle in suspension = when the flow velocity exceeds the fall velocity

Begin of sediment transport (erosion) = when the bed shear stress exceeds a critical Shield's stress

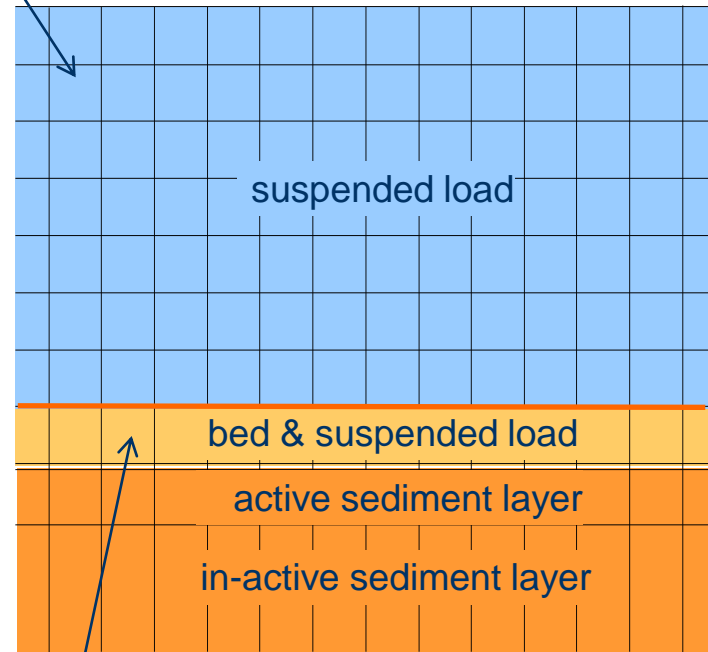
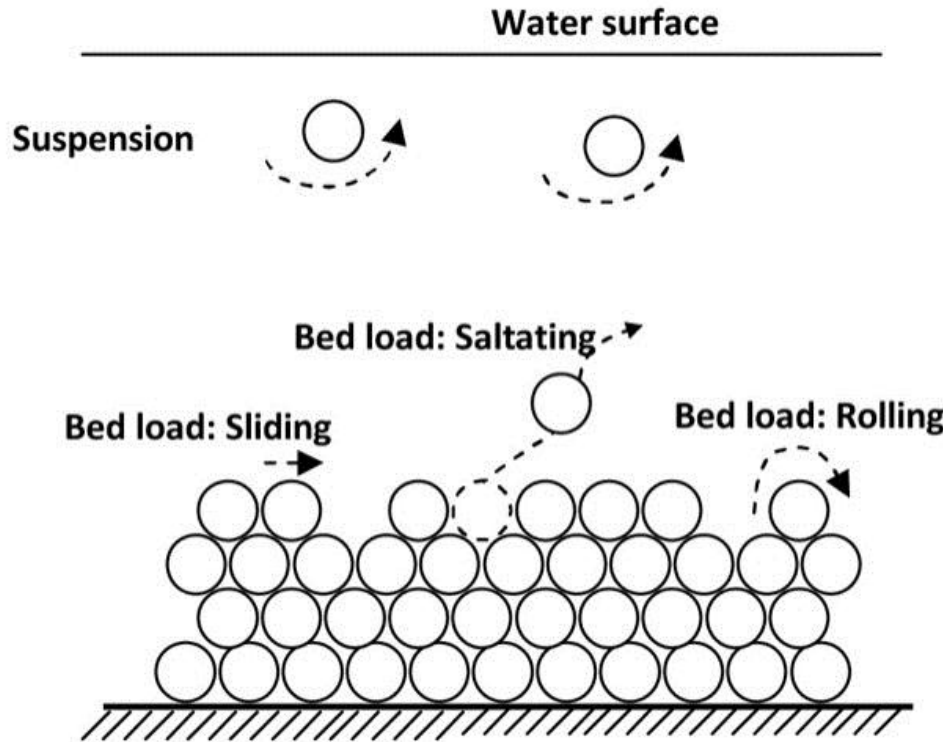


$c$  = Sediment concentration  
 $\Gamma$  = Diffusion coefficient

Convection-diffusion equation for suspended sediment:

$$\frac{\partial c}{\partial t} + U_j \frac{\partial c}{\partial x_j} + w \frac{\partial c}{\partial x} = \frac{\partial}{\partial x_j} \left( \Gamma \frac{\partial c}{\partial x_j} \right)$$

Fall velocity



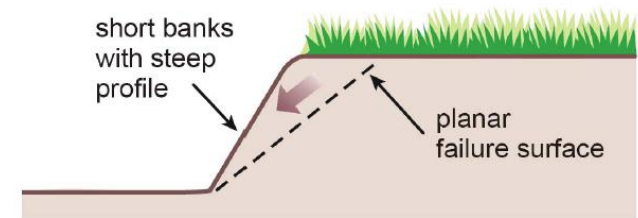
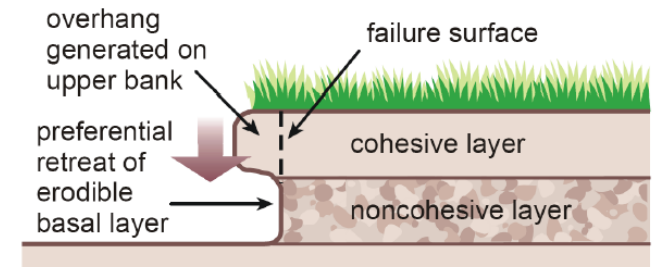
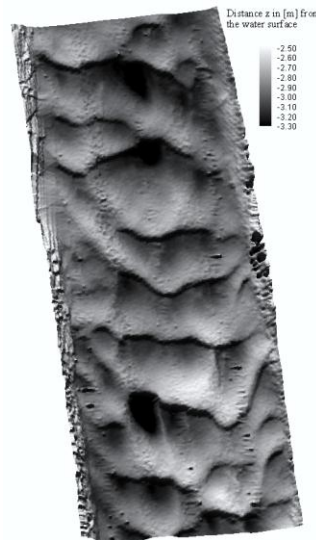
Empirical formula (Van Rijn) for the equilibrium sediment concentration close to the bed

$$c_a = 0.015 \frac{D_{50}}{a} \frac{T^{1.5}}{D_*^{0.3}}$$



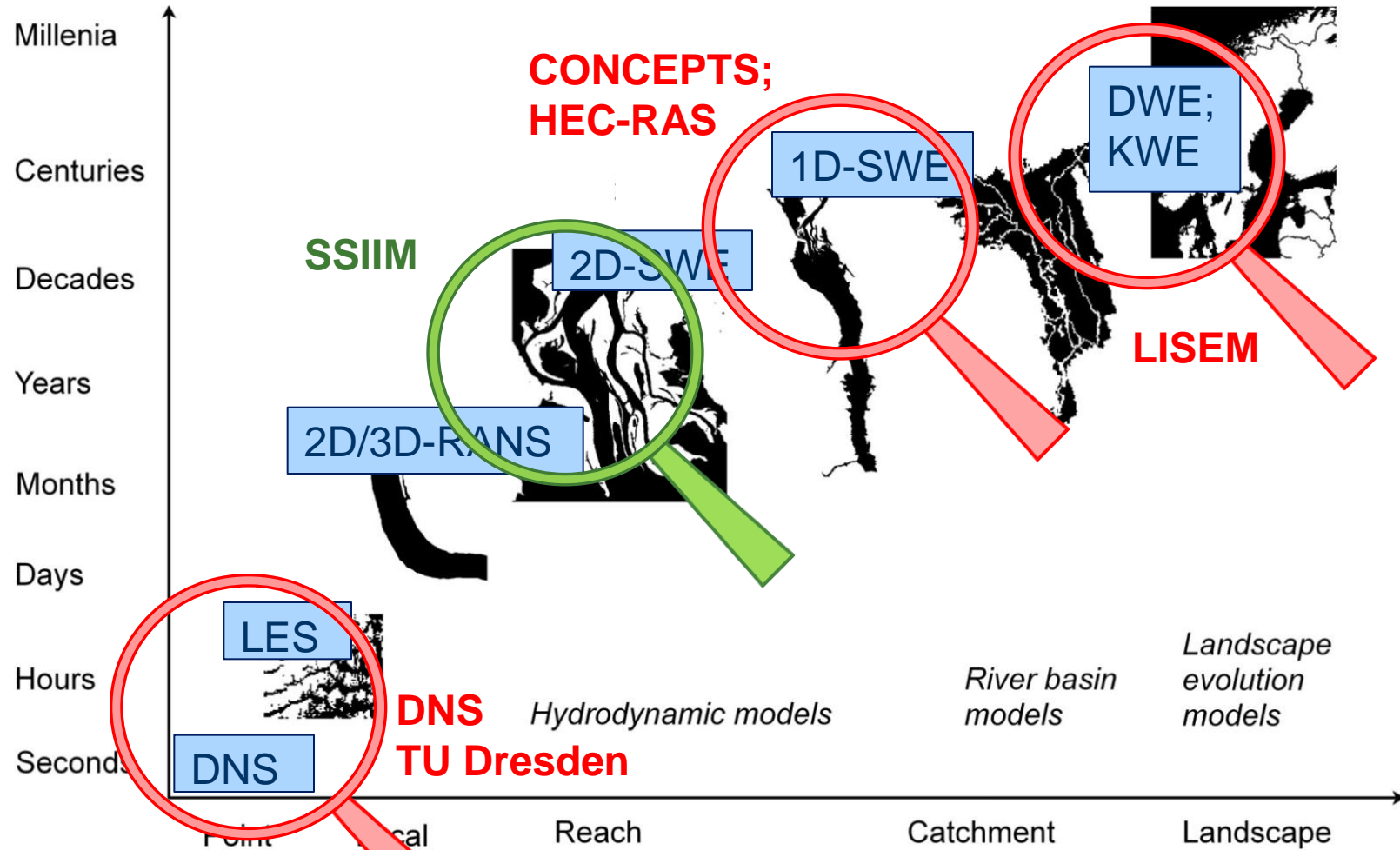
## Sediment processes:

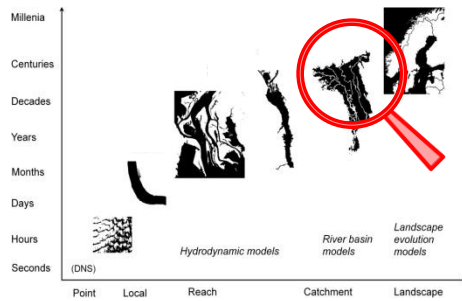
- Much less understood
- Many different approaches, often based on empirical formulas
- Large differences between sand-bed rivers and gravel-bed rivers
- High uncertainties



- Sediment transport functions
- Cohesion / coagulation of fine sediments
- Interaction between grain sizes (Hiding-exposure, sorting .... )
- Bank failure
- .....

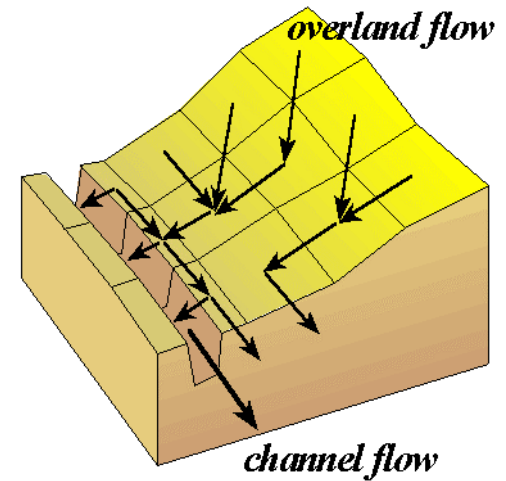
### 3. Some examples for flow and sediment models



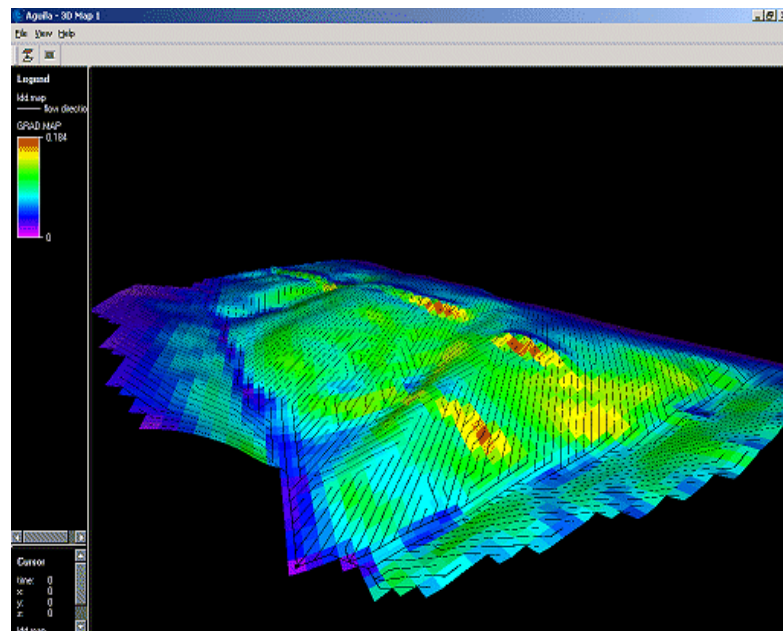


## LISEM

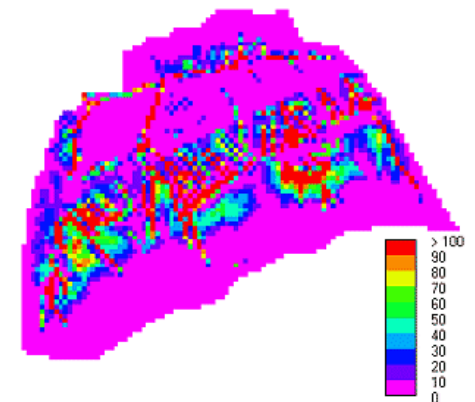
Overland and channel flow routing:  
Manning's eq. + Kinematic wave



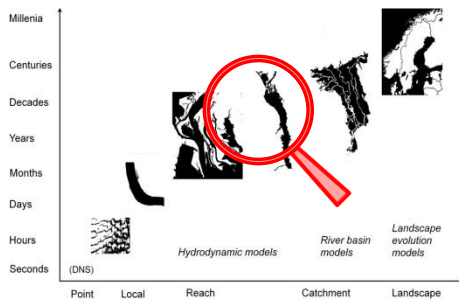
The net sediment in suspension is transported between gridcells with the kinematic wave.



Output:  
Erosion and  
deposition maps

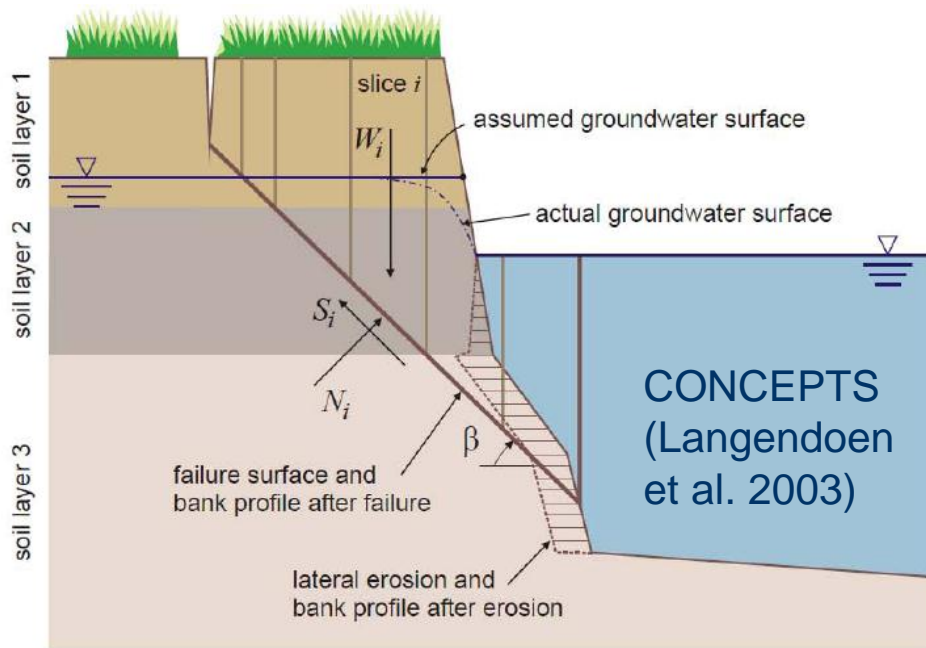
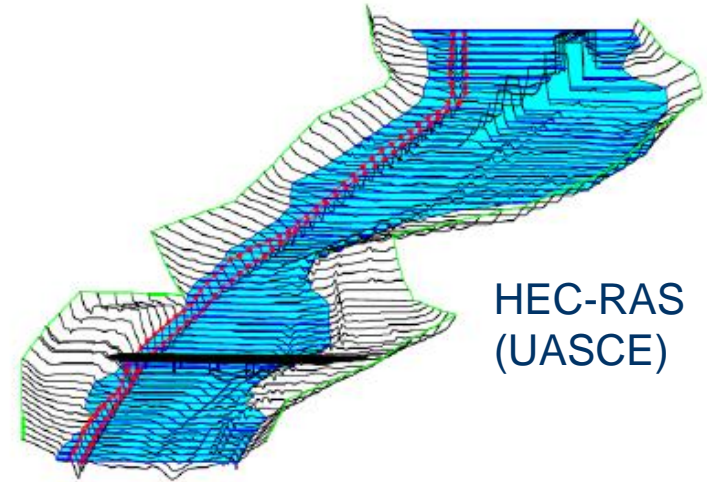




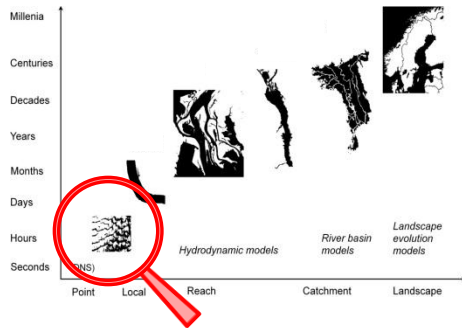


## 1D Models

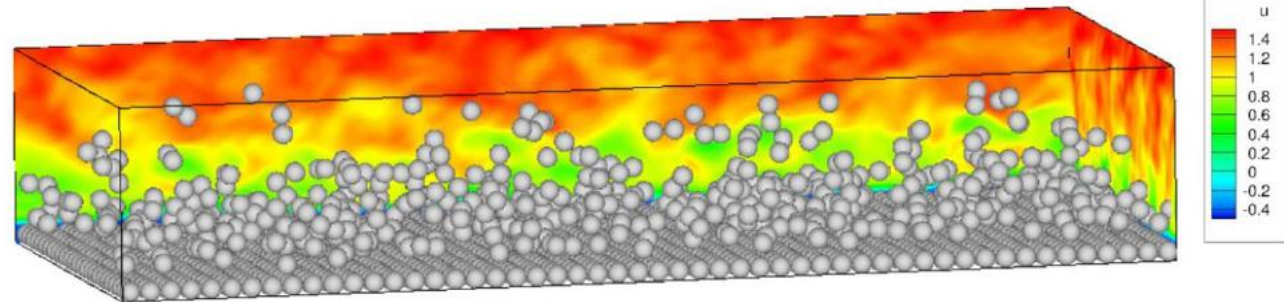
Examples for unsteady 1D flow models with sediment transport



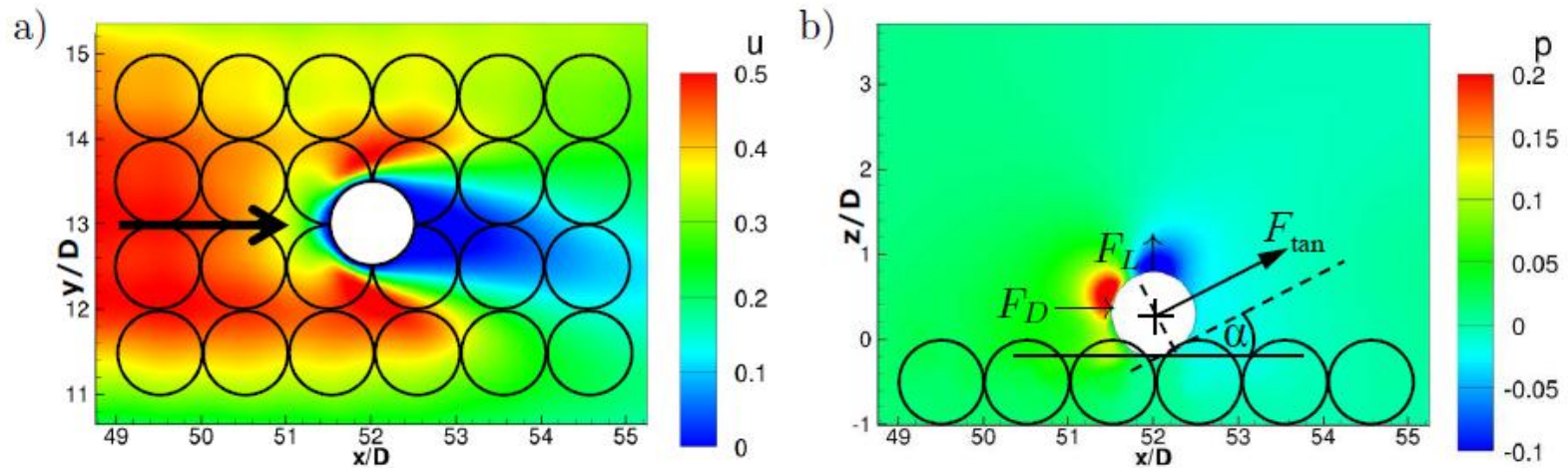
Sediment modelling feature	HEC-RAS 6	CONCEPTS
Several grain sizes	X	X
Tracking bed changes	X	X
Susp. & bed load	X	X
Cohesive and non-cohesive sed.	X	X
Sorting & Armoring	X	?
Stream bank failure		X



## Direct Numerical Simulation (DNS)

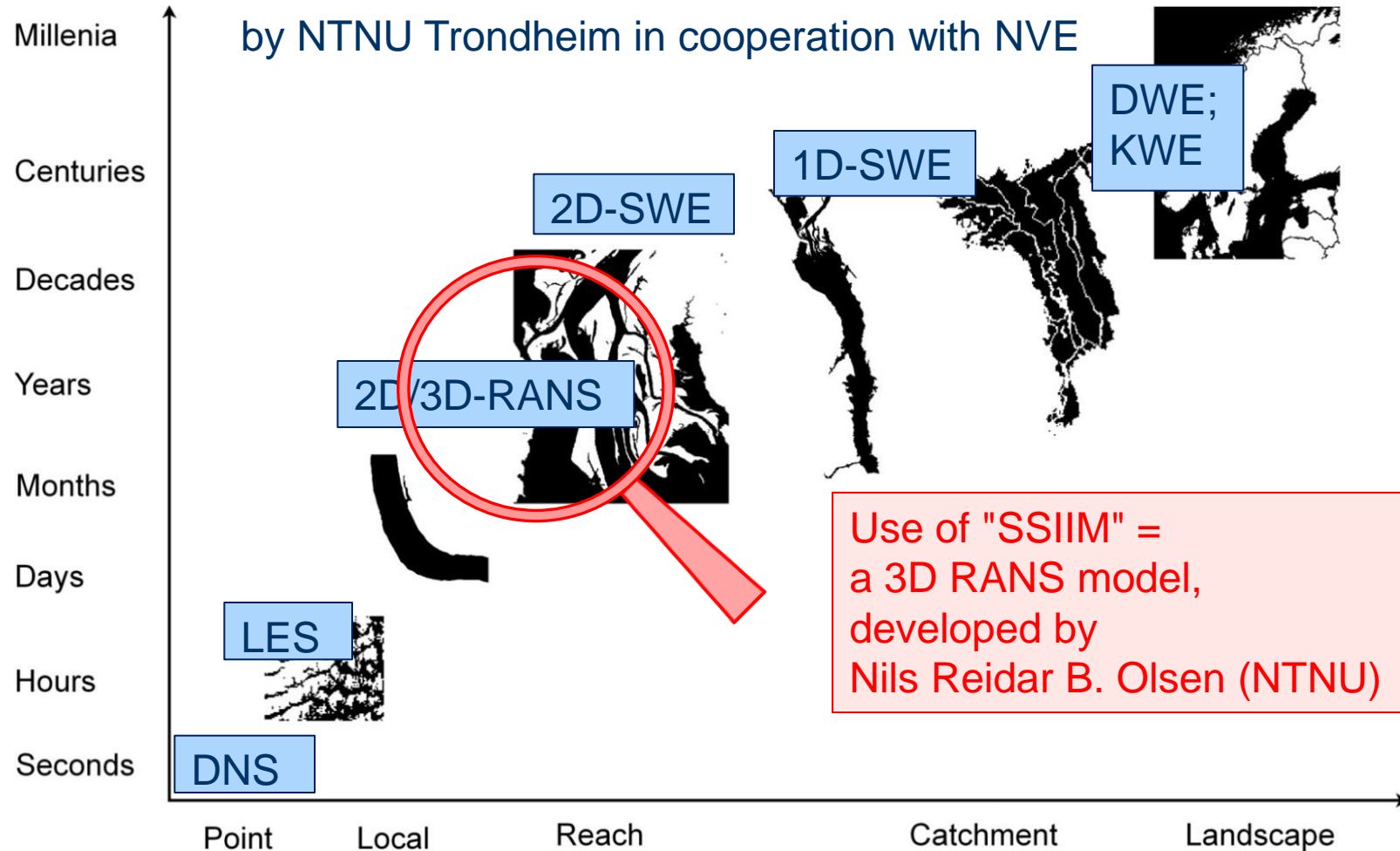


Herwig et al. 2011; Vowinkel et al. 2011



Resolving the flow field around each single particle;  
Each grain is directly moved by the calculated flow forces

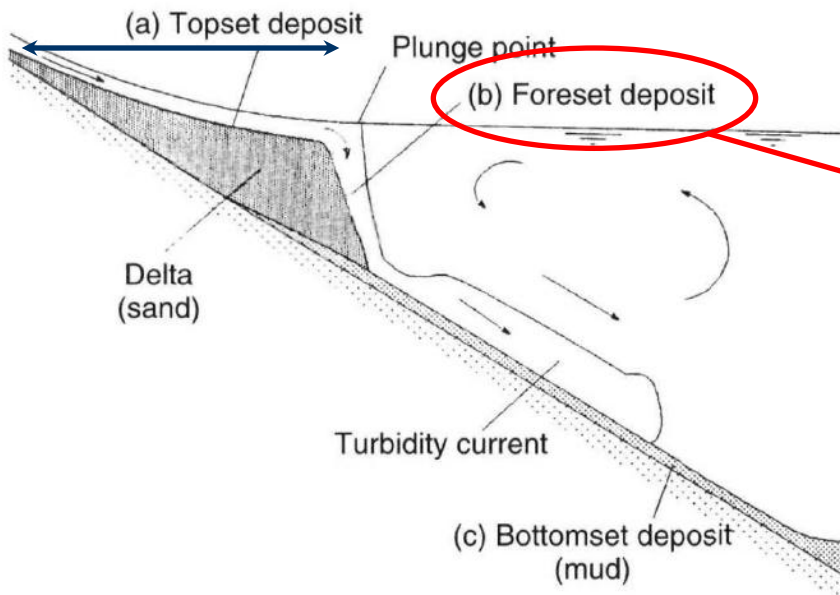
## 4. RANS Modelling study for Lake Øyeren's delta



# 4. RANS Modelling study for Lake Øyeren's delta

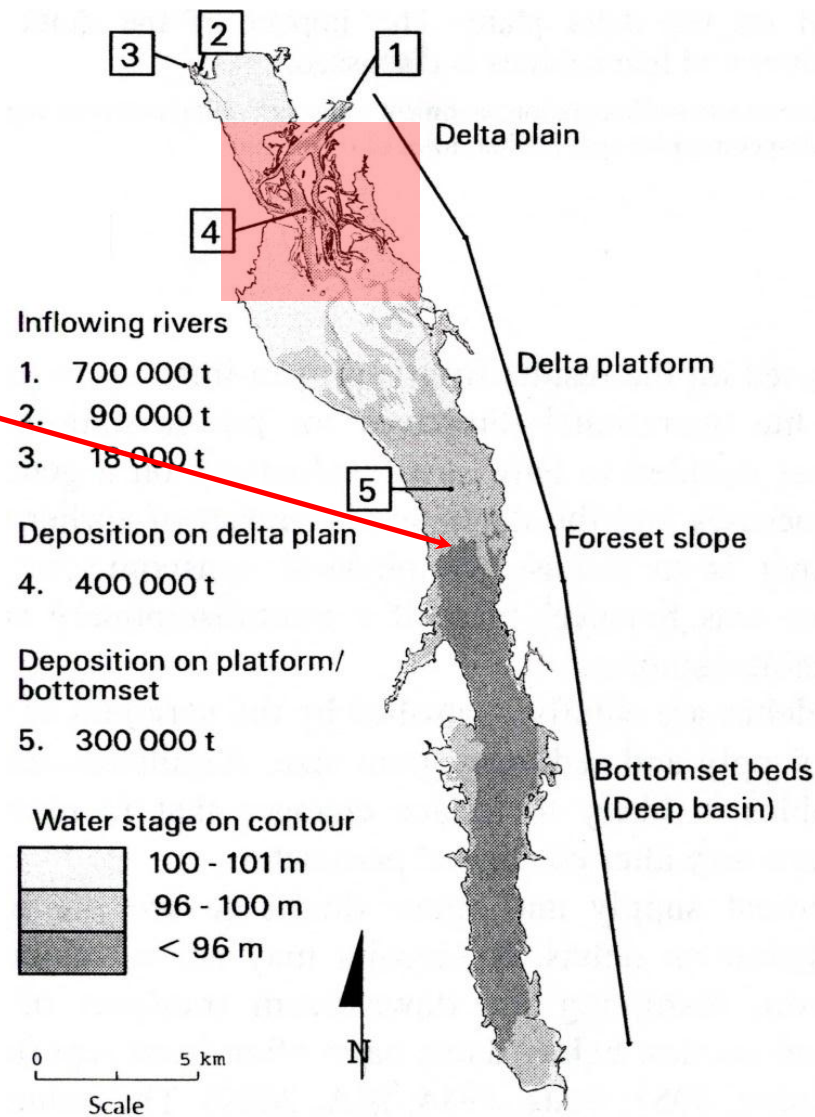
## Morphological features of the delta

### Delta plain and platform



Structure of a deltaic deposit in a lake or reservoir (Kostic & Parker 2003)

**In this work, we investigated only processes on the delta plain!**



Bogen & Bønsnes (2002)





Under mean conditions

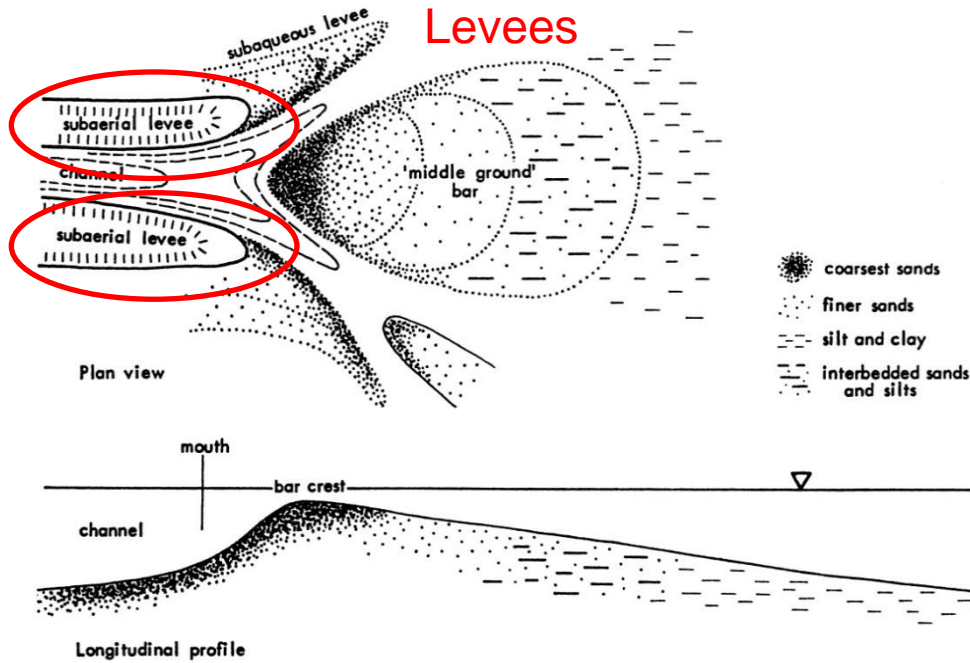


During the 1995 flood

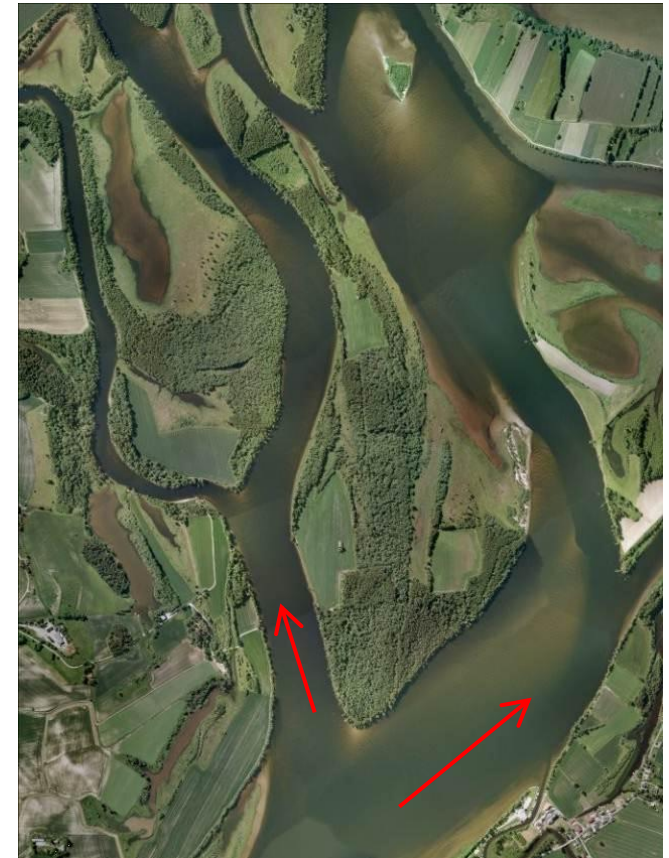
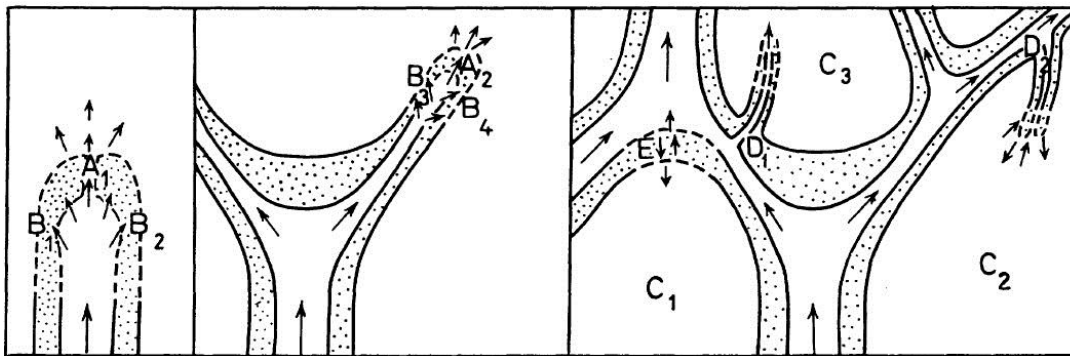


During the winter lowering

Foto: Eielinger Wilove AS ©



## Morphological processes on the delta plain



Levee deposition = an important process for delta formation and development





Sediments deposited by the flood 1995

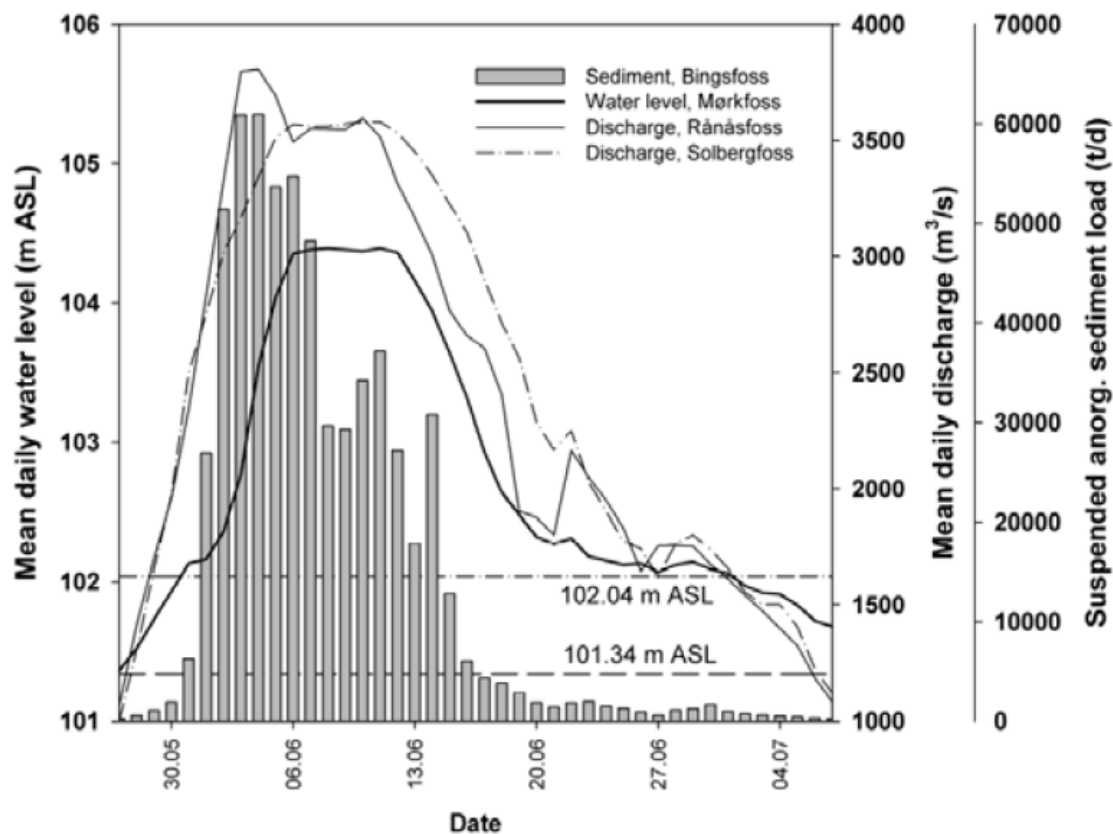
Øyeren's delta, 6. Juni 1995  
(Water level 104,35 m a.s.l.)



## 4. RANS Modelling study for Lake Øyeren's delta



Sedimentation heights 1995  
(Bogen et al. 2002)

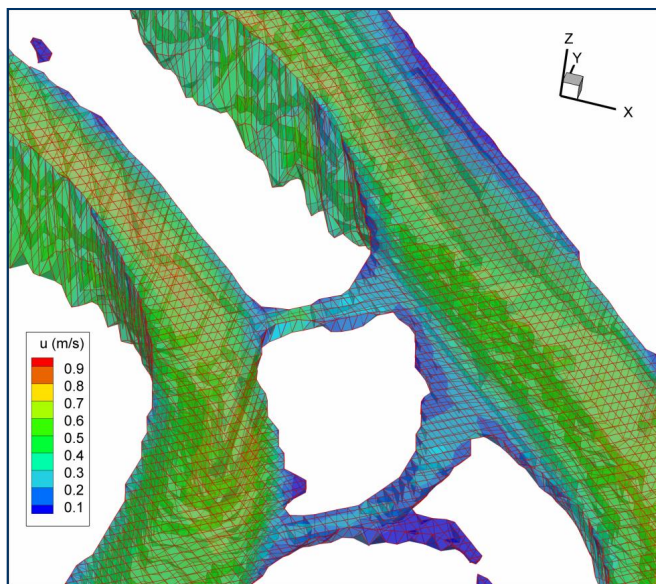


Water and sediment time curves during the 1995 flood  
(NVE Database)

### How good can we model the levee depositions of 1995?



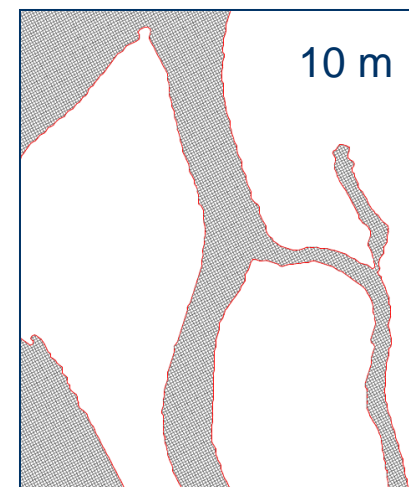
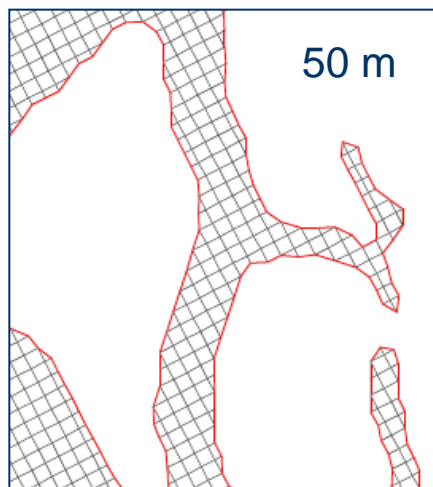
## 4. RANS Modelling study for Lake Øyeren's delta



The choice of the mesh size – a balance between the quality of the input data, the processing power of the computer and the accuracy of the numerical solution

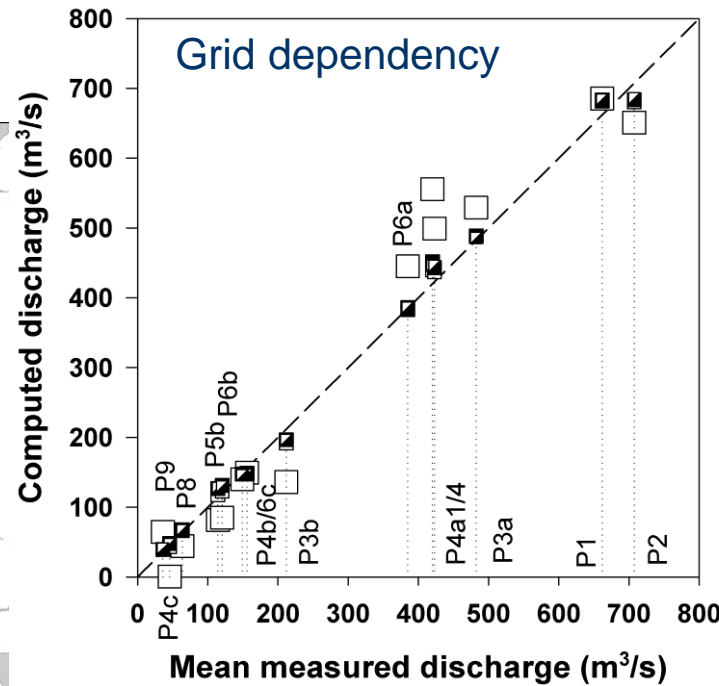
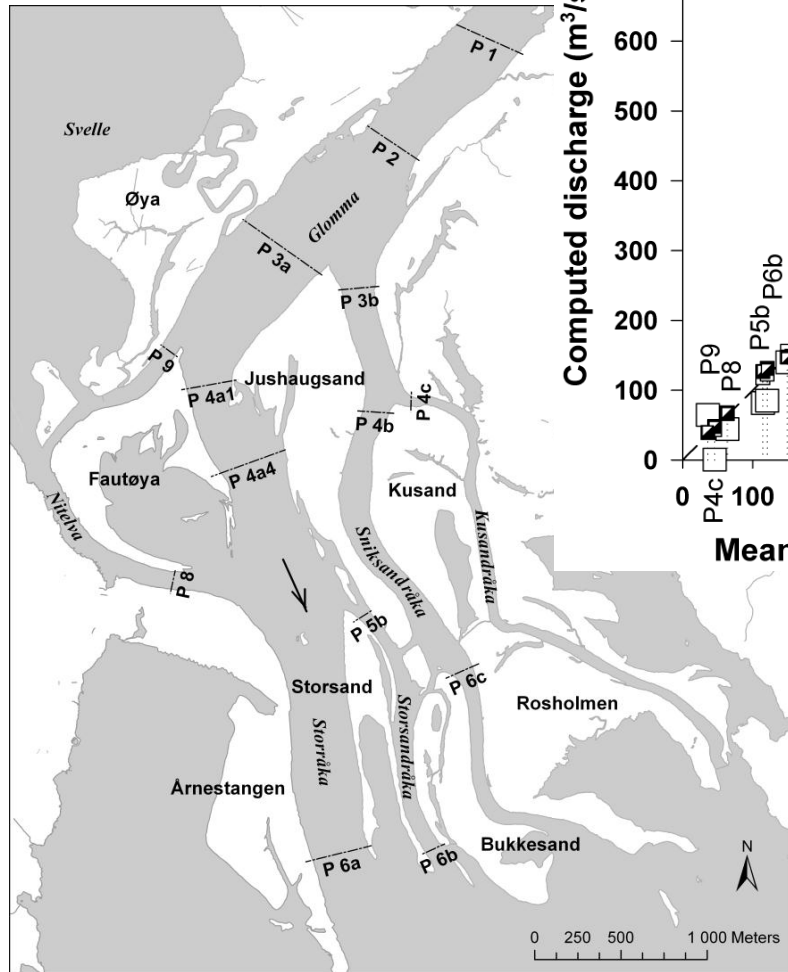
Number of grid cells for the 10 m mesh shown:  $1.7 \cdot 10^6$   
(computational time on a 16 processor 1.9 GHz IBM Power PC node: 2 to 17 hours for a stationary computation, 2-3 weeks for a flood simulation, 2009)

Spatial structure of the grid for lake stage 101.37 m a.s.l.

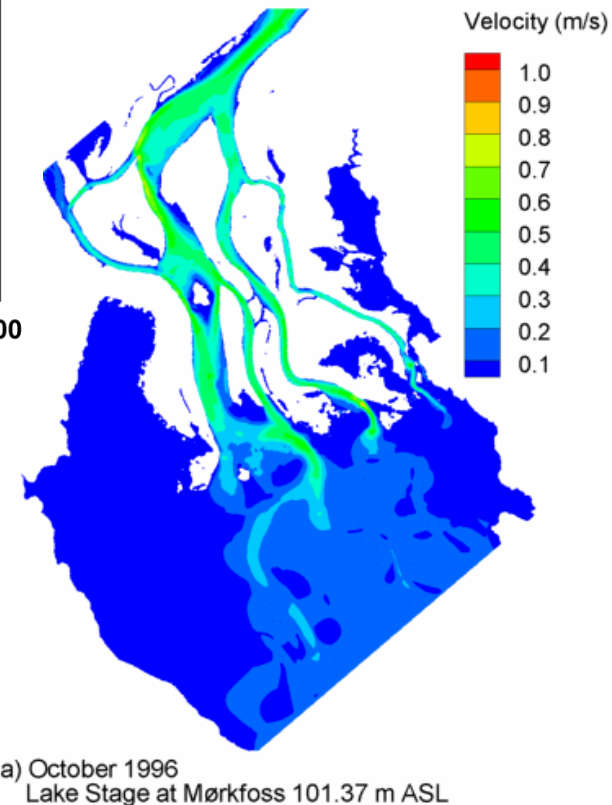


# 4. RANS Modelling study for Lake Øyeren's delta

NVE's ADCP measurement cross-sections



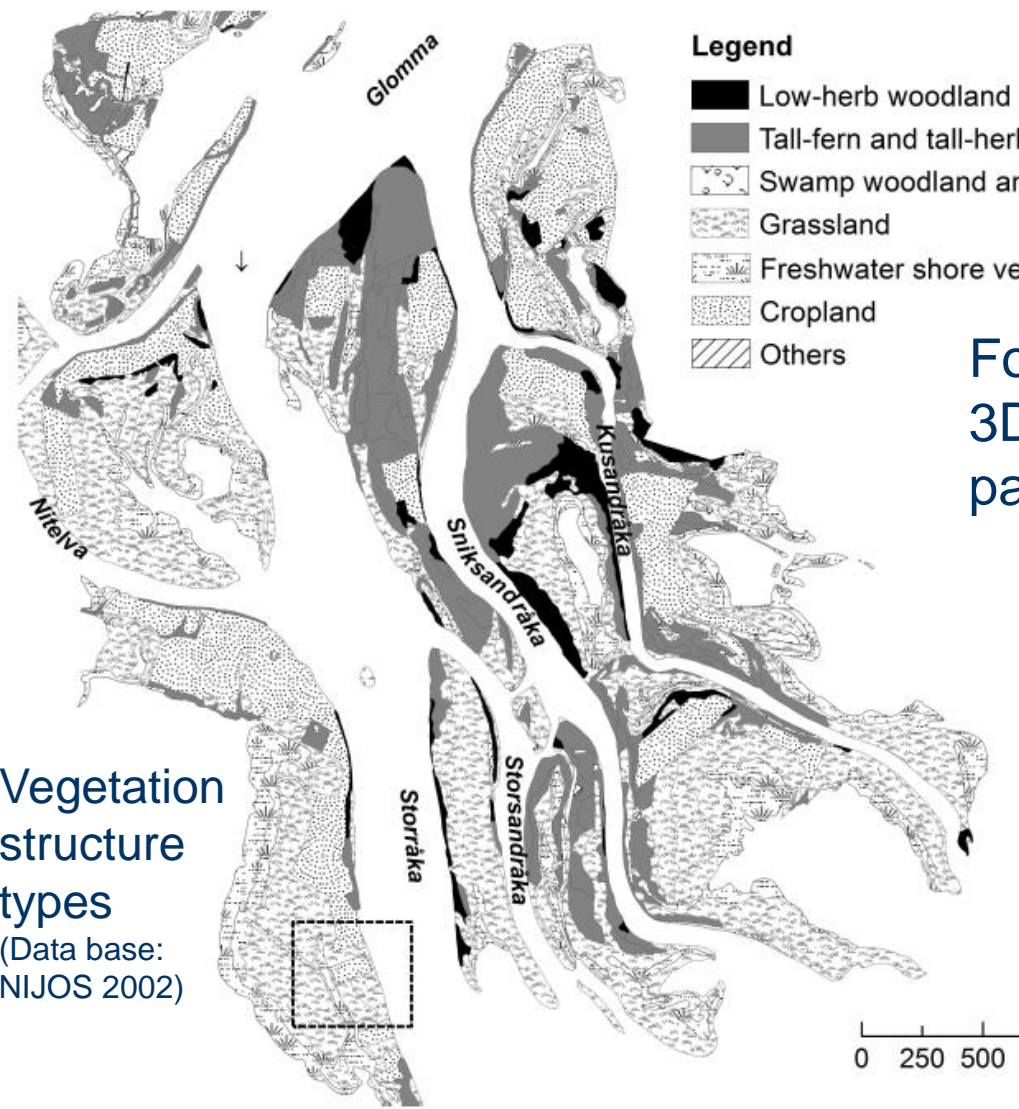
Comparison of model results with measured discharges and water levels for 3 flow situations



Set-up and calibration of the flow model (Zinke et al. 2010)



# 4. RANS Modelling study for Lake Øyeren's delta

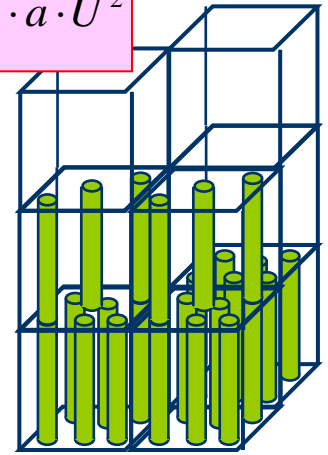


Vegetation structure types  
(Data base: NIJOS 2002)

- Legend**
- Low-herb woodland
  - Tall-fern and tall-herb woodland
  - Swamp woodland and scrub
  - Grassland
  - Freshwater shore vegetation
  - Cropland
  - Others

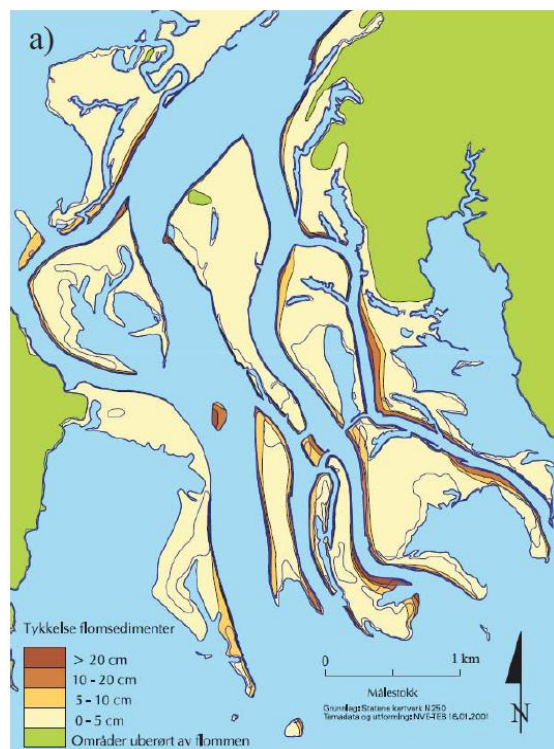
$$F_{cell} = \frac{1}{2} \rho \cdot C_D \cdot a \cdot U^2$$

For the flood case:  
3D vegetation parameters needed

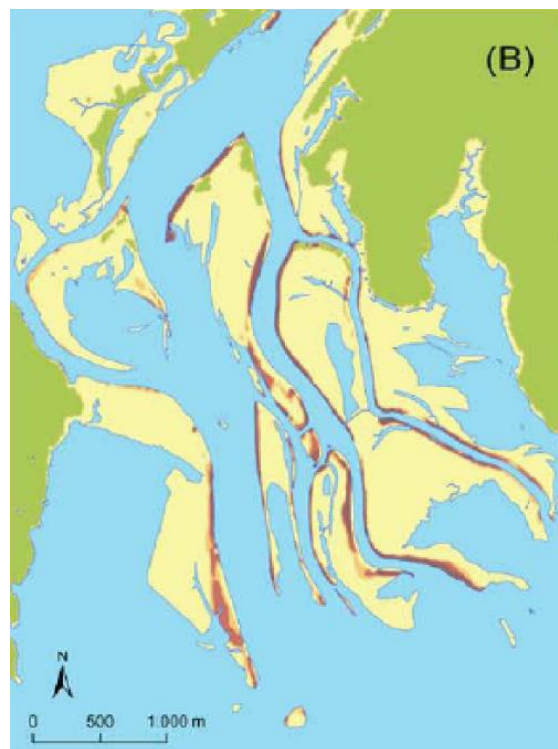


## 4. RANS Modelling study for Lake Øyeren's delta

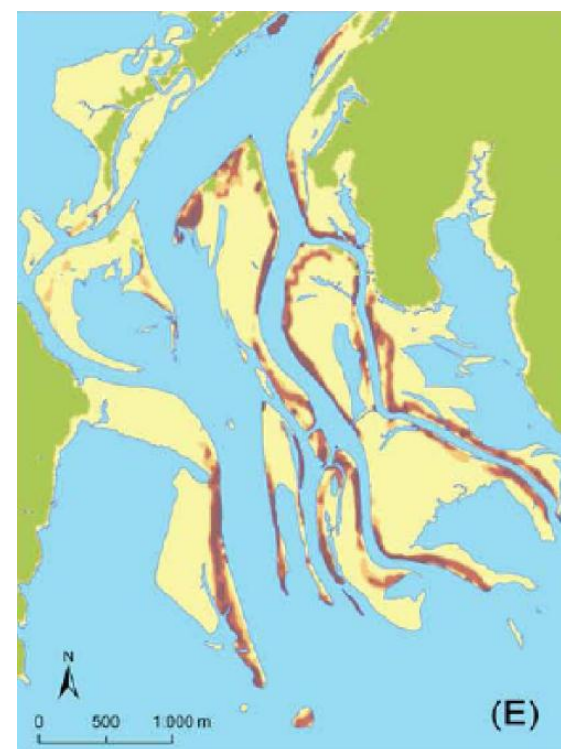
Measurements



Baseline data set



Case "No vegetation"

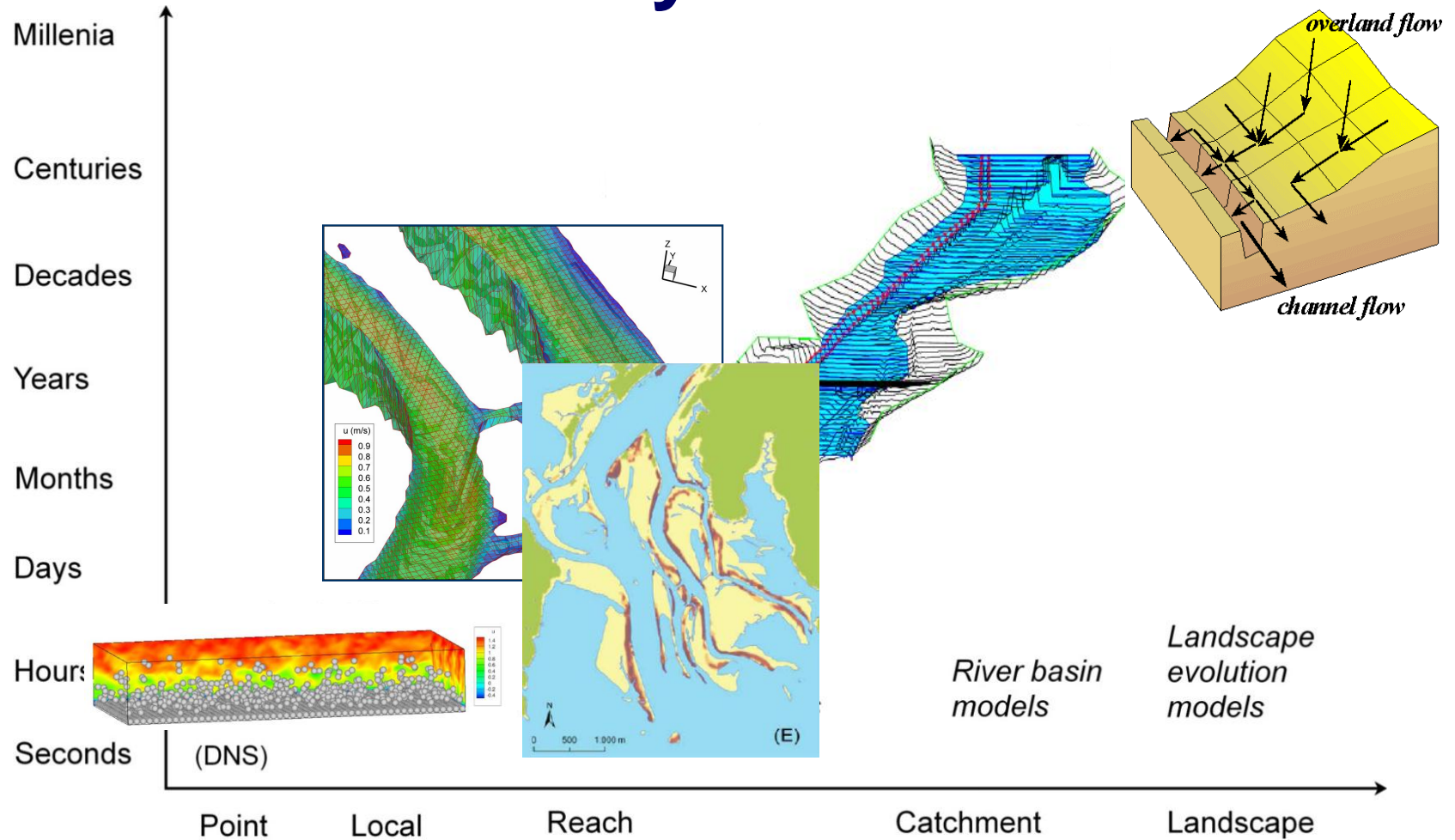


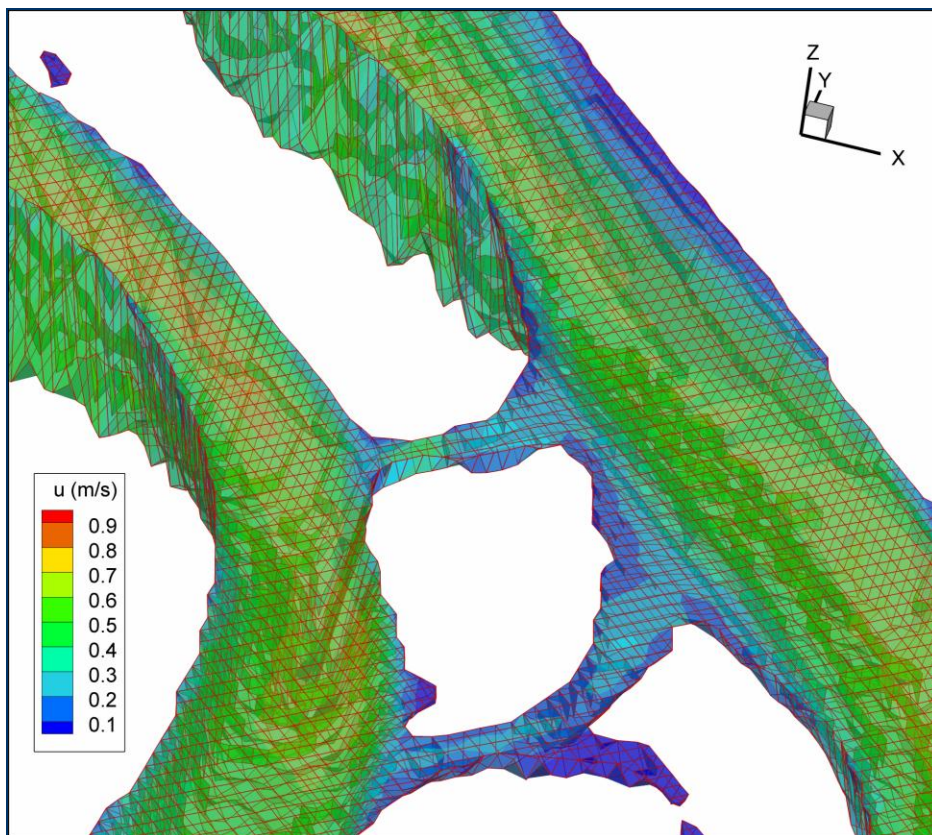
Measured and computed island deposits for the 1995 flood (Zinke et al. 2011)

Uncertainties about vegetation parameters and modelling approaches:  
one of the key factors for the modelling of levee depositions!



# 5. Short Summary





# Thank you!

Many thanks to the CFD group at NTNU-IVM Trondheim and all research partners!

## Contact:

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Water Resources Research Group

Trondheim

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